A New Feature Selection Method based on Intuitionistic Fuzzy Entropy to Categorize Text Documents

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Abstract

Selection of highly discriminative feature in text document plays a major challenging role in categorization. Feature selection is an important task that involves dimensionality reduction of feature matrix, which in turn enhances the performance of categorization. This article presents a new feature selection method based on Intuitionistic Fuzzy Entropy (IFE) for Text Categorization. Firstly, Intuitionistic Fuzzy C-Means (IFCM) clustering method is employed to compute the intuitionistic membership values. The computed intuitionistic membership values are used to estimate intuitionistic fuzzy entropy via Match degree. Further, features with lower entropy values are selected to categorize the text documents. To find the efficacy of the proposed method, experiments are conducted on three standard benchmark datasets using three classifiers. F-measure is used to assess the performance of the classifiers. The proposed method shows impressive results as compared to other well known feature selection methods. Moreover, Intuitionistic Fuzzy Set (IFS) property addresses the uncertainty limitations of traditional fuzzy set.

Keywords

High Dimensionality, Feature Selection, Intuitionistic Fuzzy Entropy, Text Categorization.

I. Introduction

In recent years, rapid development in internet technology generated massive amount of text documents by private and public sectors. To handle such a huge amount of text documents, automatic text categorization has become a popular technology to manipulate and manage [1][2]. Text Categorization (TC) is a process of automatically categorizing unknown text documents into one or more pre-defined classes by their contents. TC has been successfully proposed for many applications viz., retrieving useful information in search engines, spam filtering, document organization, automatic document indexing etc. Due to these applications automatic text categorization is an important research area in text mining and information retrieval [3][4]. Text categorization process includes feature extraction, pre-processing, feature selection and categorization. In feature extraction, the features are extracted from the text documents [5]. Each term (word) of the text document is considered as a feature and most of the features are unwanted and irrelevant. Further, during pre-processing, tokenization, stop-word elimination and stemming are employed to eliminate irrelevant and unwanted features [6]. The pre-processed text documents are represented in machine understandable form by employing a representation model. Then, feature selection method selects the most informative features from the representation model [7]. Feature selection plays high influence on the performance of classifiers and it is mainly used for dimensionality reduction [8][9]. Finally, selected feature subset is fed into a classifier to categorize the text documents. The text categorization suffers from high dimensionality of feature space. Due to this, the performance of the classifiers degrades and also takes more time for categorization [10][11]. The reduction of high dimensional feature matrix is a significant challenge in text categorization. To tackle this challenge, many researchers have proposed various feature selection methods [8-9][12-15]. Feature selection methods are generally partitioned into 3 groups: filter, wrapper and hybrid [11][15]. Presently there are various feature selection methods reported in the literature viz., Document Frequency [14], Term Frequency-Inverse Document Frequency [16], Term Strength [14], Mutual Information [17], Information Gain [18], Chi-Square [11][13], Ambiguity Measure [19], Term Frequency-Relevance Frequency [20], Symbolic Feature Selection [21], Distinguish Feature Selection [12], Entropy based Feature Selection [22] and many more. Among these feature selection methods, entropy based feature selection method computes the amount of uncertainty and the quality of information content present in the text. The concept of entropy was introduced by Shannon [23] and is called as Shannon entropy (information entropy). It is fundamentally based on information theory, which estimates the entropy value of each feature using probability. A lower value of entropy indicates higher contribution of information in decision making process and larger value of entropy indicate lesser contribution of information. The concept of entropy is described in several manners and applied in different areas [24].

The extended version of Shannon entropy is fuzzy entropy, which is non-probabilistic entropy [25]. It adopts a new term named match-degree to estimate entropy value [26][27]. Match degree satisfies the four properties of de Luca-Termini axioms [25][27]. The probability of the entropy is computed using the number of occurring terms. In

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contrast, the match degree in fuzzy entropy is computed using the membership values of the occurring terms [26]. The fuzzy entropy value does not only consider the number of features, but also considers the actual distribution of features by membership function. Hence, fuzzy entropy reflects more information in the actual distribution of the features than Shannon entropy in the feature space [27].

Fuzzy Entropy is based on the fuzzy set, which measures the fuzziness. The Fuzzy set is used to solve various real world problems, which mainly deals with imprecisionness and vagueness [29]. In fuzzy set theory, the membership value of a feature varies between 0 to 1. Fuzzy set assumes that the non-membership is complementary of membership, but in real world this assumption fails due to hesitation. This hesitation originates, while defining the membership function, due to lack of precise knowledge and it is another type of uncertainty. To address this hesitation, Atanassov [30] developed an Intuitionistic Fuzzy Set (IFS), which is an enhanced version of Fuzzy Set. Unlike Fuzzy set which considers only the membership degree, the IFS considers the degree of non-membership and the hesitation along with degree of membership. In IFS, the degree of non-membership is less than or equal to the complement of the degree of membership due to the hesitance degree. The IFS gives mathematical model to deal with the vagueness arising from the inherent uncertainty and imprecision or insufficiency of imperfect information. Considering these advantages, many researchers have recently developed IFS based clustering techniques. Chaïra [31] proposed a novel Intutionistic fuzzy c-means (IFCM) clustering method. IFCM gives more accurate clusters, and shows better performance in the presence of uncertainty and it clusters the data with less iteration than the traditional FCM [32].

Motivated by the significant advantages of IFCM and Fuzzy Entropy, in this article a new feature selection method called Intuitionistic Fuzzy Entropy-Feature Selection (IFE-FS) is proposed for text categorization. This method selects feature subsets based on intuitionistic fuzzy entropy for text document categorization. Basically, it contains two phases: In the first phase, Intuitionistic membership degree is computed with the help of the IFCM clustering method. In second phase, the Intuitionistic fuzzy entropies on the basis of the Intuitionistic membership degree via match degree are estimated. Further, entropy values are arranged in ascending order and then the feature subset selection is pruned by the threshold value. Finally, selected feature subset is considered as input to the classifiers to categorize the text documents. More popular classifiers such as K-Nearest Neighbor (KNN) [33], Support Vector Machine (SVM) [34] and Radial Basis Function-Neural Network (RBFNN) [35] are used. These classifiers are used due to their widespread use in the area of text mining and give competitive results on standard benchmark datasets [33]. The proposed method is experimented on 3 standard benchmark datasets viz., 20 Newsgroups, Reuters-21578 and TDT2. The performance of IFE-FS method is compared with CHI-Square (χ2) [11], Mutual Information (MI) [7], Information Gain (IG) [18] and Entropy based Feature Selection (EFS) [22]. All these feature selection methods have their variant characteristics and also are the well-known feature selection methods for text categorization.

The main contribution of this article is as follows:

1. Proposes a new feature selection method (IFE-FS) based on Intuitionistic Fuzzy Entropy, which reduces high dimensionality of feature matrix and enhances the performance of classifiers.
2. Resolves uncertainty (hesitation) limitation of Fuzzy Entropy by making use of IFS.
3. Conducts extensive experiments on three standard benchmark datasets. The experimental results acknowledge that the IFE-FS method shows outstanding performance in terms of F-measure.

The rest of the article is organized as follows: existing and entropy based feature selection methods are reviewed in section II. The preliminary outlines on the Intuitionistic fuzzy set are presented in section III. The proposed method (IFE-FS) along with illustration is described in detail in section IV. The experimental results and discussion are presented in section V. Finally, the conclusion along with future work is presented in section VI.

II. Literature Review

High dimensionality of the feature matrix is a major challenge during text categorization. Feature selection plays an effective role to identify the relevant features to minimize dimensionality. Feature selection method gives reduced text feature collection, reduces storage size, lesser model building and computation time, and better model interpretation [9][15][36]. However, many studies [37][38][39] indicate that there are no feature selection methods to provide accurate discriminative feature for text categorization. Given the importance of feature selection for text categorization, many methods were proposed and some of them are presented below.

Recent researchers adopted the concept of entropy in feature selection methods to select the discriminate features. The concept of Entropy is based on the information theory proposed by Shannon which is also called as Shannon Entropy [23]. It measures the expected uncertainty of probability distribution with the results predicted by random experiments. Tang et al., [40] proposed a feature selection method based on the information theory, which uses Jeffreys-Multi-Hypothesis (JMHI) divergence information measure. This method ranks the original features and maximizes the discriminative capacity for text categorization. Largeron et al., [22] proposed a feature selection method called Entropy based Category Coverage Difference (ECCD), which is based on the entropy. This method computes the occurrence of terms inside various classes with the assistance of entropy. Cai and Song [41] used the maximum entropy modeling with different feature selection methods to categorize text documents and also proposed novel feature selection method named as “count difference”. This method considers features of both relevant and irrelevant classes to compute the frequency differences between relative documents. Vaghela et al., [42] presented an entropy based feature selection method, which uses InfoDist and Pearson’s Correlation parameters. This method selects the features using InfoDist, which adopts conditional entropy to compute the relevancy of feature and category. Further, it eliminates the irrelevant features using Pearson’s correlation. Liu and Song [43] presented the portion set of key words based on proximity degree. Key words are selected based on entropy, semantic field and association degree. Later, fuzzy classification is used to categorize documents.

Many researchers have identified the significance of entropy and have developed fuzzy entropy measures from various perspectives [44]. Fuzzy entropy has been widely used in pattern recognition, image processing and clustering analysis. De and Termini [25] proposed the first non-probabilistic entropy based on the fuzzy set theory. Khushaba et al., [45] described the fuzzy entropy in terms of match degree. The fuzzy entropy uses match degree instead of probability to estimate value of the entropy. Parkash et al., [46] used the principle of maximum weighted fuzzy entropy to develop two new weighted fuzzy entropy measures to remove the redundancy. Luukka [47] proposed a feature selection method based on fuzzy entropy, in which fuzzy entropy is estimated by using the membership degree in fuzzy set. This method minimizes the dimensionality of feature space and also enhances the efficiency of classifiers. Ahmadizar et al., [48] proposed a hybrid feature selection method, which has two stages. In the first stage, dimensionality of the feature matrix is reduced using the fuzzy entropy feature selection method. Fuzzy entropy values are ranked in ascending order and then the feature subset with lowest entropy value is selected. In the second stage, ant colony optimization is used to
select the features from feature subset for text categorization.

All the above mentioned methods fail to handle uncertainty that arises while defining the membership function. To handle this uncertainty, Atanassov [30] developed Intuitionistic Fuzzy Set (IFS) in 1986, which is an advanced version of fuzzy set. IFS considered degree of non-membership and hesitation along with degree of membership. In IFS, non-membership degree is computed by employing intuitionistic fuzzy complement generator [49][50]. Intarapaiboon [51] proposed a framework for text categorization based on similarity measure of intuitionistic fuzzy sets. In this framework, each document is represented in terms of the IFS, where the IFS uses sugeno’s integral method to represent the document. Different types of similarity measures using IFS are described in [52][53]. Szmidt and Kacprzyk [54] proposed a feature selection method based on the IFS for text categorization. This method uses the degree of membership, non-membership and hesitation to resolve the imbalance and overlap class problem of categorization.

Chaina [31] proposed a novel Intuitionistic fuzzy c-means (IFCM) clustering method. The IFCM was evaluated on various CT scan brain images and achieved better performance than Type 2 fuzzy and traditional Fuzzy C-means algorithms. In literature, many researchers applied IFCM clustering method to solve image processing problems [55-58]. However, very less amount of work is reported on text categorization [51][54]. In addition to clustering methods, researchers developed entropy methods based on IFS. Szmidt and Kacprzyk [59] depicted entropy as far as non-probabilistic type of entropy. Burillo and Bustince [60] depicted entropy as far as degree of intuitionism of an intuitionistic fuzzy set. Hung and Yang [61] proposed two IFS based entropy measures and provided the axiomatic definition of entropy for IFS. Vlachos and Sergiadis [62] proposed new Intuitionistic Fuzzy Entropy and also presented the connection between intuitive and mathematics of entropy for fuzzy set and IFS.

From literature survey, it is observed that a lot of work is reported on entropy and fuzzy entropy based feature selection methods for text categorization. In addition, it is also observed from the literatures that IFS addresses the limitation of fuzzy set by considering the hesitation degree. In this article, we developed a new Feature Selection method based on Intuitionistic Fuzzy Entropy (IFE). To the best of our knowledge this work is first of its kind, where a feature selection method based on IFE to categorize the text documents is proposed. The next section describes the construction of Intuitionistic Fuzzy Set for IFCM.

### III. Construction of Intuitionistic Fuzzy Set (IFS)

In this section, the mathematical background on IFS is explained. The Intuitionistic Fuzzy Set, in general sense is portrayed by the membership degree, the non-membership degree and the hesitation degree [30].

Generally the fuzzy set \( A \) is defined on text document \( D_i \) as

\[
A = \{ (T_j, \mu_s(T_j)) | T_j \in D_i \}
\]

Where, \( \mu_s(T_j) \rightarrow [0,1] \) denotes the membership degree of \( A \). \( T_j \) is the \( j \)-th feature in the \( i \)-th document \( D_i \). The membership value \( \mu_s(T_j) \) defines the degree of belongingness of \( T_j \in D_i \) in \( A \). An Intuitionistic fuzzy set \( \tilde{A} \) is described on document \( D_i \) as:

\[
\tilde{A} = \{ (T_j, \mu_s(T_j), \theta_s(T_j)) | T_j \in D_i \}
\]

Where, \( \mu_s(T_j) \) and \( \theta_s(T_j) \) denotes membership and non-membership degree of \( j \)-th feature \( T_j \) respectively. In the fuzzy set, another uncertainty emerges while defining the membership function due to imprecise knowledge. IFS handles this uncertainty by considering the hesitation degree. Unlike in fuzzy set, where the non-membership degree is calculated by taking the complement of membership degree, IFS computes the non-membership degree with the help of intuitionistic fuzzy complement generator. In this work, the Sugeno’s intuitionistic fuzzy complement generator is used to calculate the non-membership degree [49]. The Sugeno’s intuitionistic fuzzy complement is computed as

\[
\theta_s(T_j) = \frac{1 - \mu_s(T_j)}{1 + \lambda \mu_s(T_j)} \quad (3)
\]

Where, \( \lambda \) is the constant and \( \lambda > 0 \). When we set \( \lambda = 1 \), IFS becomes the traditional fuzzy set. Hesitation degree of a term \( T_j \in D_i \) is computed as

\[
\pi_s(T_j) = 1 - \mu_s(T_j) - \theta_s(T_j) \quad (4)
\]

Where \( \pi_s(T_j) \) is the hesitation degree of \( j \)-th feature \( T_j \). It is evident from the equation (4)

\[
0 \leq \pi_s(T_j) \leq 1, \quad \forall T_j \in D_i
\]

Non-membership degree is computed from Sugenio’s intuitionistic fuzzy complement. Thus, using Sugeno’s intuitionistic fuzzy complement, the IFS becomes

\[
\tilde{A}_i = \left\{ (T_j, \mu_s(T_j), \frac{1 - \mu_s(T_j)}{1 + \lambda \mu_s(T_j)}) | T_j \in D_i \right\}
\]

### IV. Proposed Method

A new feature selection method based on Intuitionistic Fuzzy Entropy (IFE) named as Intuitionistic Fuzzy Entropy-Feature Selection (IFE-FS) is proposed in this section. The Intuitionistic Fuzzy Entropy estimates the value of entropy on the basis of intuitionistic membership degree via match degree. The intuitionistic membership degrees are computed from the Intuitionistic Fuzzy C-Means (IFCM) Clustering method. The IFCM is based on the Intuitionistic Fuzzy Set (IFS), which considers the degree of membership, non-membership and hesitation. The proposed method consists of two phases: in the first phase, an intuitionistic membership value is computed using IFCM. In the second phase, entropy is estimated using the intuitionistic membership values and a feature subset is selected on the basis of the entropy value.

#### A. Intuitionistic Fuzzy C-Means (IFCM) Clustering Method

Intuitionistic Fuzzy C-Means (IFCM) is an advanced version of the traditional Fuzzy C-means (FCM) and it is based on the IFS. Unlike, FCM which clusters input document based on the membership value, IFCM considers the non-membership and hesitation degree along with the membership degree.

Let us assume that there are \( k \) number of pre-defined classes \( C_x, x = 1,2,3,...,k \). Each class contains \( n \) number of documents \( D_{x,i}, i = 1,2,3,...,n, \) and \( m \) number of features (terms) \( T_{j,i}, j = 1,2,3,...,m \).

Then the total number of documents is denoted by \( z = [k \times n] \). The text document contains sequence of terms (features), where each term is treated as a feature. In text document, most of the features are irrelevant and redundant. These features results in high dimension in feature space and also degrade the performance of classifier. It is necessary to use pre-processing techniques to eliminate irrelevant and redundant features. The most common pre-processing task is
The IFCM optimizes the objective function by continuously updating the membership degree and the cluster center until it meets the convergence criteria value \( \varepsilon \), i.e., \( |J^{(t)} - J^{(t-1)}| < \varepsilon \). Here, \( t \) is the iteration and \( \varepsilon \) is the user-specified convergence criteria. Further, using this membership value, match degree is computed to estimate the entropy.

**B. Intuitionistic Fuzzy Entropy (IFE)**

The Intuitionistic Fuzzy Entropy is the non-probabilistic entropy in which we use match degree to estimate the entropy value. The match degree in IFE is computed using the intuitionistic membership value. IFE maximizes the capacity of discriminative features and generates more affluent information. Match degree is described as

\[
X_a = \sum_{i=1}^{m} \mu_a(T_i)
\]

(12)

Where, \( \mu_a(T_i) \) indicates the membership of \( l \)th feature \( T_i \) in \( a \)th class \( C_a \). The match degree \( X_a \) is the ratio of intuitionistic membership of each feature \( T_i \) in class and by the summation of intuitionistic membership of feature \( T_i \) in all classes. The match degree \( X_a \) in intuitionistic fuzzy entropy uses the membership values to calculate the matching degree of feature in class. Later the Intuitionistic fuzzy entropy (IFE) of feature \( T_i \) in class \( C_a \) is computed using the following equation

\[
IFE_{a} = -X_a \log X_a
\]

(13)

Further, each features' IFE value of class is summed to calculate the overall Intuitionistic fuzzy entropy of each feature

\[
IFE_a = \sum_{a=1}^{k} IFE_{a}
\]

(14)

The lower entropy value of a feature indicates major contribution about the classes. Therefore, we select \( r \) number of low ranked features. Here, the threshold value \( r \) indicates the number of features selected and also \( r \) varies depending on the datasets. But during experimentation, the major issue is in choosing an accurate threshold value. It will be varied multiple times before selecting the best value. The selected feature subset is then given to the classifiers to categorize the text documents. We used three different classifiers: K-Nearest Neighbor (KNN), Support Vector Machine (SVM) and Radial Basis Function Neural Network (RBF-NN). The performance of IFE-FS method is measured based on the F-measure. Algorithm 1 explains the individual steps involved in the proposed method.

In order to provide more meaningful theory of our proposed method, the next section illustrates the proposed method in detail by considering a simple term document matrix.
TABLE I. TERM DOCUMENT MATRIX (TDM)

<table>
<thead>
<tr>
<th>Documents</th>
<th>$T_1$</th>
<th>$T_2$</th>
<th>$T_3$</th>
<th>$T_4$</th>
<th>$T_5$</th>
<th>$T_6$</th>
<th>$T_7$</th>
<th>$T_8$</th>
<th>$T_9$</th>
<th>$T_{10}$</th>
<th>Classes</th>
</tr>
</thead>
<tbody>
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<td>3</td>
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<td>0</td>
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<td>1</td>
<td></td>
<td></td>
<td></td>
</tr>
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<td>3</td>
<td>0</td>
<td>0</td>
<td>0</td>
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<td></td>
<td></td>
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</tr>
<tr>
<td>$D_3$</td>
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</tr>
<tr>
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<td>1</td>
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<td>1</td>
<td>0</td>
<td></td>
<td></td>
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<td></td>
</tr>
<tr>
<td>$D_6$</td>
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</tr>
</tbody>
</table>

TABLE II. CLUSTER CENTERS

<table>
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<tr>
<th>$D_1$</th>
<th>$D_2$</th>
<th>$D_3$</th>
<th>$D_4$</th>
<th>$D_5$</th>
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<th>$D_7$</th>
<th>$D_8$</th>
<th>$D_9$</th>
<th>$D_{10}$</th>
<th>Classes</th>
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<tbody>
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<td>0.8542</td>
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<td>1.3264</td>
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<td>1.3980</td>
<td>$C_3$</td>
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TABLE III. MEMBERSHIP DEGREE MATRIX

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<th>$T_3$</th>
<th>$T_4$</th>
<th>$T_5$</th>
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<th>$T_7$</th>
<th>$T_8$</th>
<th>$T_9$</th>
<th>$T_{10}$</th>
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TABLE IV. NON-MEMBERSHIP DEGREE MATRIX

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<th>$T_9$</th>
<th>$T_{10}$</th>
<th>Classes</th>
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</table>

C. Illustration

This section illustrates the individual steps involved in the proposed feature selection method. For illustration we considered an example of Term Document Matrix (TDM) of size $10 \times 8$, where $10$ documents (D) are distributed among $3$ classes (C) with $8$ unique features (T). The same is presented in Table I.

The proposed feature selection method is based on the Intuitionistic Fuzzy Entropy, which uses the Intuitionistic Fuzzy C-Means (IFCM) clustering method to compute the intuitionistic membership degree for entropy estimation. So we computed each features’ membership degree rather than that of the documents in all classes. The objective function of IFCM is shown in equation (7).

Algorithm 1: Intuitionistic Fuzzy Entropy Feature Selection (IFE-FS)

**Data:** $k$ Number of class with $n$ number of documents and $m$ number of terms (features), Fuzzy Coefficient ($p$), Convergence Criteria ($\varepsilon$), $\lambda$ is constant and Threshold ($r$)

**Result:** Class label

**Step 1:** Initialize cluster centers $v_j$, randomly

**Step 2:** Compute membership degree using equation (8)

**Step 3:** Compute non-membership degree using equation (9)

**Step 4:** Compute hesitation degree using equation (10)

**Step 5:** Compute Intuitionistic Fuzzy membership degree using equation (7)

**Step 6:** Compute Intuitionistic Fuzzy cluster center using equation (11)

**Step 7:** Compute objective function using equation (6)

**Step 8:** Compute match degree using equation (12)

**Step 9:** Compute class-wise Intuitionistic Fuzzy entropy for each feature using equation (13)

**Step 10:** Compute overall Intuitionistic Fuzzy entropy for each feature using equation (14)

**Step 11:** Select feature subset by using Threshold value ($r$)

**Step 12:** Selected feature subset will be the input to classifiers
In this illustration, the algorithm converges in the 32nd iteration. The final Intuitionistic membership values and cluster centers are shown in Table X and Table XI respectively and the objective function value is 76.6067.

In step 8, the final Intuitionistic membership values are given to the match degree to compute the actual distribution of features with respect to the class by using equation (13). The obtained match degree of the feature is shown in Table XII.

In step 9, class-wise Intuitionistic Fuzzy Entropy is estimated for each feature with respect to the class by using equation (14) and the estimated entropy value are presented in Table XIII. Later, all rows are summed up to compute the overall Intuitionistic Fuzzy Entropy for each feature by using equation (15), which is shown in Table XIV with a dimension of $1 \times 8$.

The obtained entropy value of each feature is sorted in ascending order to select the features with lower entropy values, which is shown in Table XV. The features are ranked $T_1 > T_2 > T_3 > T_4 > T_5 > T_6 > T_7 > T_8$ based on their entropy value. The lower entropy
value indicates higher relevant feature with respect to the class and contributes with more information. The higher entropy value indicates less contribution to the class. Thus, we select lower entropy values for categorization.

In next step, we select the number of features based on Threshold value \(r\). The Threshold value \(r\) is used to prune the feature subset. The \(r\) value is selected after multiple iterations by considering distinct values for \(r\) times and we found that \(r=3\) is the most suitable value for the given illustration. Here \(r\) value is less than total number of features. The selected discriminative features are presented in Table XVI.

Finally, the selected feature subset is considered as the input to the classifiers to categorize the text documents.

V. Experiments

This section presents detailed experimentations carried out to demonstrate the efficiency of the proposed method.

A. Datasets Description

In order to assess the effectiveness of the Intuitionistic Fuzzy Entropy-Feature Selection (IFE-FS) method, experiments are conducted on 20-Newsgroups [63], Reuters-21578 [64] and TDT2 [65] standard benchmark datasets. The 20-Newsgroups dataset is a set of 18846 online newsgroup documents, split evenly into 20 different classes with 26214 features. The Reuters-21578 dataset is from newswire, which contains 8293 documents and is non-uniformly divided into 65 categories with 18933 features. The TDT2 (Topic Detection and Tracking) dataset consists of 9394 documents and 36771 features, spread across 30 categories. In each dataset, distribution of features is varied according to their corresponding classes.

B. Experimental Setup

During the experimentation, it is necessary to split the dataset into training and testing set (to validate the proposed method). The large training data results in overfitting of the model. On the other hand, small training data results in underfitting the model. The whole reason for split comes from the fact that, we often have limited and finite data. So we want to make the best use of it and train on as much data as we can. In this paper, to validate the proposed IFE-FS method, we split the dataset into training and testing set in 60:40 ratios respectively. The training set is 60% documents of each class of dataset, used to build our proposed method. On the other hand, 40% testing set is applied on proposed model to assess the performance.

The performance of the proposed method mainly depends on the IFCM parameter values. Authors in [31] investigated the parameter values of IFCM. Based on the backdrop of [31], in this paper we initialized the parameters as follows: fuzzy coefficient \(P=2\), convergence criteria \(\varepsilon=0.0001\) and \(\lambda=0.5\). The performance of the IFE-FS method is compared against the four widely used feature selection methods viz., Chi-Square, Mutual Information (MI), Information Gain (IG) and Entropy based Feature Selection (EFS). We conducted experiments on three standard benchmark datasets using KNN, SVM, and RBF-NN classifiers. We used the F-Measure metric to assess the performance of the classifiers. The F-Measure is widely used in text categorization, which indicates the overall categorization performance and also combined effectiveness measure determined by precision and recall.

| TABLE XII. MATCH DEGREE MATRIX |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| \(T_1\)  | \(T_2\)  | \(T_3\)  | \(T_4\)  | \(T_5\)  | \(T_6\)  | \(T_7\)  | \(T_8\)  |
| 0.7467 | 0.1616 | 0.6273 | 0.2249 | 0.2733 | 0.3135 | 0.1517 | 0.4597 | \(C_1\) |
| 0.1266 | 0.4197 | 0.1864 | 0.3874 | 0.3631 | 0.3433 | 0.4244 | 0.2701 | \(C_2\) |
| 0.1265 | 0.4186 | 0.1861 | 0.3876 | 0.3635 | 0.3431 | 0.4237 | 0.2701 | \(C_3\) |

| TABLE XIII. INTUITIONISTIC FUZZY ENTROPY |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| \(T_1\)  | \(T_2\)  | \(T_3\)  | \(T_4\)  | \(T_5\)  | \(T_6\)  | \(T_7\)  | \(T_8\)  |
| 0.0946 | 0.1279 | 0.1270 | 0.1457 | 0.1539 | 0.1579 | 0.1242 | 0.1551 | \(C_1\) |
| 0.1136 | 0.1582 | 0.1359 | 0.1595 | 0.1597 | 0.1594 | 0.1579 | 0.1535 | \(C_2\) |
| 0.1136 | 0.1583 | 0.1359 | 0.1595 | 0.1597 | 0.1593 | 0.1580 | 0.1535 | \(C_3\) |

| TABLE XIV. OVERALL INTUITIONISTIC FUZZY ENTROPY |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| \(T_1\)  | \(T_2\)  | \(T_3\)  | \(T_4\)  | \(T_5\)  | \(T_6\)  | \(T_7\)  | \(T_8\)  |
| 0.3219 | 0.4444 | 0.3989 | 0.4648 | 0.4734 | 0.4767 | 0.4402 | 0.4622 |

| TABLE XV. FEATURES RANKED IN ASCENDING ORDER |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| \(T_1\)  | \(T_2\)  | \(T_3\)  | \(T_4\)  | \(T_5\)  | \(T_6\)  | \(T_7\)  | \(T_8\)  |
| 0.3219 | 0.3989 | 0.4402 | 0.4444 | 0.4622 | 0.4648 | 0.4734 | 0.4767 |

| TABLE XVI. SELECTED DISCRIMINATIVE FEATURES |
|-----------------|-----------------|-----------------|
| \(T_1\)  | \(T_2\)  | \(T_3\)  |
| 0.3219 | 0.3989 | 0.4402 |
A number of features are selected based on the threshold value \( r \), where \( r \) indicates the number of features. Initially, we conducted experiments by fixing \( r \) value as 500 empirically. Further, we varied the value of \( r \) from 500 to 7000, with an increment of 500. However, decrease in the value of \( r \) below 500 and increase in value of \( r \) above 7000, does not yield good results. Hence, we restricted the value of \( r \) between 500 to 7000.

### C. Experimental Results

Initially, we conducted the experiment without employing feature selection method. The number of features obtained for 20-Newsgroups is 26214, for Reuters-21578 there is 18933 and TDT2 has 36771 features. The F-measure using KNN, SVM and RBF-NN classifiers on three standard benchmark datasets are presented in Table XVII.

Fig. 1 depicts the categorization performance of the proposed method (IFE-FS) using KNN classifier in terms of F-measure on 20-NewsGroups dataset. It can be observed that each feature selection method obtained their best results with a variant number of features, in terms of F-measure. The IFE-FS method achieved better result of 0.662 for 2500 features compared to other feature selection methods using KNN classifier. Our proposed feature selection method identifies discriminative features when the value of \( r \) is 2500, which leads to achieve the maximum result. Similarly, we conducted the same set of experiments using SVM and RBF-NN classifiers on 20-NewsGroups.

![Fig. 1. Performance comparisons using KNN classifier (20-NewsGroups dataset).](image1)

![Fig. 2. Performance comparisons using SVM classifier (20-NewsGroups dataset).](image2)

![Fig. 3. Performance comparisons using RBF-NN classifier (20-NewsGroups dataset).](image3)

Fig. 2 and Fig. 3 show the performance comparison of the IFE-FS method with existing feature selection methods on 20-NewsGroups for SVM & RBF-NN classifier. The proposed IFE-FS method performed better compared to existing feature selection methods, when the number of features are ranging from 4500 to 7000. In Fig. 3, the performance of RBF-NN based on MI, IG and Entropy, completely coincides with each other. However, the F-measure curve of RBF-NN based on the proposed IFE-FS method is significantly higher than that of the existing feature selection methods. It is evident from Fig. 1, 2 and 3 that the performance of IFE-FS method in terms of F-measure is superior to that of the existing feature selection methods when value of \( r \) is 2500 for KNN, 5000 for SVM and 5500 for RBF-NN classifiers.

Further, the same set of experimentations were carried out on Reuters-21578 and TDT2 dataset. In Reuters-21578, the performance of the proposed IFE-FS method with that of the existing feature selection methods using KNN, SVM and RBF-NN classifiers are shown in Fig. 4, 5 and 6, respectively. It can be observed from Fig. 4-6 that the performance of the proposed IFE-FS method is lower than other feature selection methods, when the number of features ranging from 500 to 2500.

![Fig. 4. Performance comparisons using KNN classifier (Reuters-21578 dataset).](image4)
Fig. 5. Performance comparisons using SVM classifier (Reuters-21578 dataset).

Fig. 7. Performance comparisons using KNN classifier (TDT2 dataset).

Fig. 8. Performance comparisons using SVM classifier (TDT2 dataset).

Fig. 9. Performance comparisons using RBF-NN classifier (TDT2 dataset).

Fig. 6. Performance comparisons using RBF-NN classifier (Reuters-21578 dataset).

Fig. 7, 8 and 9 show the comparison of the proposed Intuitionistic Fuzzy Entropy-Feature Selection (IFE-FS) method with the existing feature selection method using KNN, SVM and RBF-NN classifiers on TDT2 dataset. It can be observed from Fig. 7-9, that the proposed IFE-FS method outperforms other existing feature selection methods. Fig. 7 shows that F-measure curve of KNN classifier based on the proposed IFE-FS method is higher than that of the other existing feature selection methods, when the value of \( r \) is ranging from 2500 to 6000. Similarly, the proposed IFE-FS method achieved best result when value of \( r \) is ranging from 3000 to 6000 using SVM. From Fig. 9, we can observe that the proposed IFE-FS method achieved best result when the value of \( r \) is in the range of 5500 and 6000 using RBF-NN classifier. The proposed IFE-FS method obtained a result of 0.837 using KNN classifier when the value of \( r \) is 3500, SVM achieved 0.915 result when the value of \( r \) is 3500 and RBF-NN achieved 0.967 result when the value of \( r \) is 5500, which are presented in Fig. 7, 8 and 9.

From Fig. 1-9, we can infer that, in terms of F-measure, the performance of IFE-FS method improved when the value of \( r \) is ranging from 2500 to 6000. In addition, the proposed IFE-FS method identifies discriminative features when the value of \( r \) is ranging from 2500 to 6000, which lead to achieve maximum result for all three classifiers. Table XVII presents the F-measure results using KNN, SVM and RBF-NN classifiers without feature selection method on the three datasets. From Table XVII and Fig. 1-9, we can observe that the result of the proposed IFE-FS method with all three classifiers is superior than the results of the same classifier without feature selection.

Besides, the following observations were made during the experimentation:

- From experimental results, it is noted that the IFE-FS method obtained better results by considering less number of features from the original feature set.
- From Fig. 1-9, the proposed IFE-FS method achieved significantly better results on all standard benchmark datasets using KNN, SVM and RBF-NN classifiers.
D. Discussions

The proposed IFE-FS method performance is measured in terms of F-Measure. It is evident from Fig. 1-9 that the proposed IFE-FS method performs superior compared to Chi-Square, MI, IG and Entropy based Feature Selection (EFS) methods using KNN, SVM and RBF-NN classifiers on the three standard datasets. The Chi-Square, estimates the lack of independence between terms and class. The proposed IFE-FS method computes the distribution of terms in each class. Thus, the proposed IFE-FS method obtained higher result than Chi-Square on all the three datasets. The MI estimates the mutual dependency of two terms using joint probability distribution and marginal probability distribution. The proposed IFE-FS method is non-probabilistic, which estimates the intuitionistic fuzzy information by intuitionistic fuzzy set. IG evaluates the quantity of bits of information acquired by knowing the presence or absence of a term in the document for categorization prediction. However, the proposed IFE-FS method does not consider absence or presence of term in a document.

On the other hand, the EFS method considers only randomness uncertainty and estimates the entropy of the terms in a class, based on probability. However, the proposed IFE-FS method considers uncertainty like randomness, ambiguity and vagueness to provide the terms with importance in the class. Moreover, it maximizes the discriminative capacity of the features and produces rich information. The proposed IFE-FS method shows higher performance using RBF-NN classifier compared to other KNN and SVM classifier. It can be concluded from the experiments that the proposed IFE-FS method shows significant improved performance using classifiers by selecting a number of discriminative features based on the distribution of terms in the classes. The proposed IFE-FS method performs better compared to other well known feature selection methods. However, the performance of the proposed method mainly depends on the number of features, initial cluster centers and parameter values. These parameter values differ across the datasets and it makes very difficult task to select the parameter values.

VI. Conclusion

In this article, a new feature selection method called Intuitionistic Fuzzy Entropy-Feature Selection (IFE-FS) is proposed for text categorization. The IFE is based on the intuitionistic fuzzy set. Unlike traditional Fuzzy Entropy, which considers only membership degree, Intuitionistic Fuzzy Entropy considers non-membership and hesitation degree along with membership degree. Thus, it handles uncertainty to better extent. To evaluate the performance of proposed IFE-FS method, extensive experimentations were conducted on three standard benchmark datasets: 20-NewsGroups, Reuters-21578 and TDT2. From the experiments, we can conclude that the IFE-FS method reduces high dimensionality of feature matrix and enhances the performance of classifier. It can also be concluded that IFE-FS selects good subsets of features, which contains most discriminative features. The experimental results reveal that the IFE-FS method outperformed other feature selection methods in terms of F-measure.

In future, we intend to use optimization technique in the proposed IFE-FS method to automatically select the threshold value r. Additionally, we intend to add the kernel method in IFCM, which could improve the categorization performance.

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